Final Exam
Mate 3048
Spring 2011

Name:
Student Number:


Instructions: Solve all problems. Even though group discussions are encouraged, the work you present here has to be your own. This work due Saturday, May $28^{\text {th }}$ at $6: 45$ PM, at Monzón 311. Not electronic submissions will be allowed. No other students can handle in your work. Fail to accomplish this requirements will render an F on this work.

1. Solve the following:
a. $\frac{d y}{d x}=\frac{x^{4}+2 y}{x}$
b. $\frac{d y}{d x}=\frac{2 x y}{y^{2}-x^{2}}$
c. $y^{\prime \prime}+y^{\prime}-2 y=4 x^{2}-10 x+1$
2. Find the curves that hit the circles $x^{2}+y^{2}=c$ in 45 degrees angles.
3. A body falls from rest subject to gravity in a medium offering resistance proportional to the Square of the velocity. Find expressions for velocity and distance.
4. Prove that: $\left(e^{a t} f\right) *\left(e^{a t} g\right)=e^{a t}(f * g)$
5. Find information about Heun's Method for approximate numerical solutions. Compare, Euler's Method, Runge Kutta Method and Heun's method to approximate $\frac{\pi}{3}$. You must mention differences in performance, precision and error analysis.
