

1. A certain sequence  $(b_n)$  satisfies the recursion

$$b_{n+1} = b_n^3 - b_n.$$

Can this sequence have limit 6? What are the possible limits of this sequence, if any? State clearly which principle enters into play.

2.  $y = f(x) = x(x - 3)$  is the equation of a parabola. Complete the square so as to put it in the form  $y = (x - a)^2 + b$ , and find, graphically, the image under  $f$  of the interval  $[-2, 2]$ . Provide an explanation of the colour code.

3.

(a) Find  $\lim_{x \rightarrow \infty} e^{-2 \log x}$ .

(b) Find  $\lim_{x \rightarrow -\infty} \frac{x^2 - 3x + 1}{2 - x}$ .

4. Plot the ceiling function  $x \mapsto \lceil x \rceil$ . According to the definition (which you must state), is it right or left continuous at the integers?
5. Find the intercept of the tangent to the ellipse of equation

$$\frac{x^2}{9} + \frac{y^2}{4} = 1$$

at the point  $(-\sqrt{27}/2, 1)$ , with the x-axis.

6. (pb 71 of § 4.4). Two people start walking from the same point. One walks west at 5 mph, the other south, at 6 mph. At what rate is the distance between them changing after 40 minutes?
7. Suppose that  $f(2) = -4, g(2) = 3, f'(2) = 2, g'(2) = -1$ . Find  $dy/dx$  for:

(i)  $y = \frac{f}{2g}$                       (ii)  $y = \frac{f(x)}{x^2 + 1}$ .