University of Puerto Rico Mayaguez Campus Faculty of Arts and Sciences

## Department of Mathematical Sciences

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## COLLOQUIUM

October 2th, 2012

## Stochastic Switching Networks of Adaptive Frequency Oscillators

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The present work belongs to the vast body of research devoted to behaviors that emerge when homogeneous or heterogeneous agents interact. We adopt a stylized point of view in which the individual agents' activities can be assimilated into nonlinear dynamical systems, each with their own set of specific parameters. Since the pioneering work of C. Huyghens in the seventeenth century it has been established that interactions between agents modify their individual evolutions — and that for ad-hoc interactions and agents that are not too dissimilar, synchronized behaviors emerge. In this classical approach, however, each agent recovers its individual evolution when interactions between them are removed or as summarized by a French aphorism: "Chasser le naturel et il revient au galop".

Contrary to classical synchronization behavior which disappears when interactions are removed, here the system self-adapts and acquires consensual values for the set of local parameters. The consensual values are definitely "learned" (i.e. they stay in consensus even when interactions are removed). We analytically show for a wide class of dynamical systems how such a "plastic" and self-adaptive training of parameters can be achieved. We calculate the resulting consensual state and their relevant stability issues. The connectivity of the network (i.e. Fiedler number) affects the convergence rate but not the asymptotic consensual values. We then extend this idea to enable adaptation of parameters characterizing the coupling functions themselves. Self-learning mechanisms simultaneously operate at the agents' level and at the level of their connections. Finally, we analytically explore a set of dynamical systems involving the simultaneous action of two time-dependent networks (i.e. where edges evolve with time). The first network describes the interactions between the state variables, and the second affects the adaptive mechanisms themselves. In this last case, we show that for ad hoc time-dependent networks, parametric resonance phenomena occur in the dynamics.

Monzón Building, Room 201, 10:45 AM Refreshments will be served 15 minutes before the colloquium, M203



