

THE DEPARTMENT OF MATHEMATICAL SCIENCES PROUDLY PRESENTS

# COLLOQUIUM

SPRING 2015

## Continuous Transformations on Banach Spaces

### Héctor Salas

Department of Mathematical Sciences  
UPR – Mayaguez



March 17, 2015

#### ABSTRACT

We will show some examples of continuous functions  $f$  on compact spaces  $K \subset \mathbb{R}^n$  for which there exists a point  $x \in K$  such that its orbit  $=: \{f^n(x) : n \in \mathbb{N}\}$  is dense in  $K$ . After a brief review of the geometry of infinite dimensional Banach spaces, we will mainly consider continuous linear transformations (bounded operators) on them. The contrast of the behavior of different classes of operators is surprising. On one hand the compact operators are the most similar ones to linear transformations on finite dimensional spaces. On the other extreme there are operators with a dense orbit. If, in addition, they have a dense set of periodic points, they are called chaotic. We will also see the concept of Frechet derivatives for non linear transformations and a brief application.

Monzón Building, Room 201, **10:45 AM**  
Refreshments will be served 15 minutes  
before the colloquium in Monzón 213

